

OPTICS

Tunable intraband optical conductivity and polarization-dependent epsilon-near-zero behavior in black phosphorus

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Black phosphorus (BP) offers considerable promise for infrared and visible photonics. Efficient tuning of the bandgap and higher subbands in BP by modulation of the Fermi level or application of vertical electric fields has been previously demonstrated, allowing electrical control of its above-bandgap optical properties. Here, we report modulation of the optical conductivity below the bandgap (5 to 15 μm) by tuning the charge density in a two-dimensional electron gas induced in BP, thereby modifying its free carrier-dominated intraband response. With a moderate doping density of $7 \times 10^{12} \text{ cm}^{-2}$, we were able to observe a polarization-dependent epsilon-near-zero behavior in the dielectric permittivity of BP. The intraband polarization sensitivity is intimately linked to the difference in effective fermionic masses along the two crystallographic directions, as confirmed by our measurements. Our results suggest the potential of multilayer BP to allow new optical functions for emerging photonics applications.

INTRODUCTION

Hyperbolic photonic materials, in which the dielectric permittivities associated with different polarization directions have opposite signs, present a unique platform to engineer extremely strong anisotropic light-matter interactions and tailor previously unexplored topological properties of light (1, 2). They can enable a wide range of phenomena such as near-field enhancement and modification of the local density of states of emitters (3), negative refraction (4), hyperlensing (5), super-Planckian thermal emission (6), sub-diffraction light confinement (7), canalization of incident energy (8), and more. Such a wide range of novel functionalities are achieved easily with a relatively new class of materials known as epsilon-near-zero (ENZ) materials (9, 10). In addition to passive artificial metamaterial ENZ-based structures based on periodically arranged metal-dielectric stacks (11), hyperbolic dispersion has also been explored for a wide range of natural materials such as graphite, hexagonal boron nitride (hBN), and WTe_2 in different spectral ranges (12–14). Despite many advances in the ability to engineer ENZ or hyperbolic metamaterials, the idea of an electrically or optically tunable on-demand hyperbolic material remains experimentally fairly unexplored and is highly attractive for the study of fundamental phenomena such as achieving active control of optical topological transitions, as well as applications in optical information processing and switching, and other functions (13, 14).

Two-dimensional electron gases (2DEGs) in atomically thin materials with strong electro-optic susceptibility offer an ideal platform to achieve highly tunable light-matter interactions (15–18). These systems have established critical metrological standards in the field

of condensed matter physics [such as the fine structure constant (19) and conductance quanta (20)] and have contributed to advances in photonics (21–23). Black phosphorus (BP), among other 2D materials, has been heavily explored as an electronic platform for high-mobility 2DEG (24–29), and while first-principle calculations have been performed for undoped BP (30), very little is known experimentally about its optical properties and their tunability. Bulk BP crystal has a puckered structure, as shown in Fig. 1A, and has an anisotropic direct bandgap that is known to markedly increase from 0.3 to 2 eV as the atomically thin limit (monolayer) is reached (31, 32). In addition, the highly anisotropic band structure and optical properties of BP are extremely susceptible to perturbations in the local dielectric environment (33), temperature (34), electron/hole concentration in the 2DEG in BP (35), electric or magnetic field (36, 37), strain (38, 39), etc. While monolayer and few-layer BP can exhibit strong light-matter interactions by virtue of excitonic resonances in the visible-near infrared (IR) (40, 41), multilayer BP holds more potential in the mid-IR because of its lower bandgap and stronger Drude weight (42). Quantum well electro-optic effects and its anisotropy near the band edge have been studied recently in some detail in multilayer BP (43–46). However, absorption below the optical gap, which should be dominated by free carriers in the 2DEG, is still experimentally poorly understood and has only been investigated theoretically so far (8, 30). The free-carrier response of doped BP films can persist up to mid-IR frequencies and can be approximated to first order by a Drude model (47, 48). Similar behavior has been observed in graphene (49), but has not been experimentally explored in BP. Knowledge about the charge dynamics can provide us with an understanding of how quasiparticles in BP respond to IR electromagnetic radiation, and the exact nature of their respective scattering and damping processes. A comprehensive understanding of the polarization-dependent, mid-IR optical properties of BP may facilitate the development of BP-based photonic devices, which hold promise for novel optoelectronic functions in emerging technology applications.

In this work, we report a comprehensive study of the optical conductivity of a 2DEG induced in multilayer BP for different hole and

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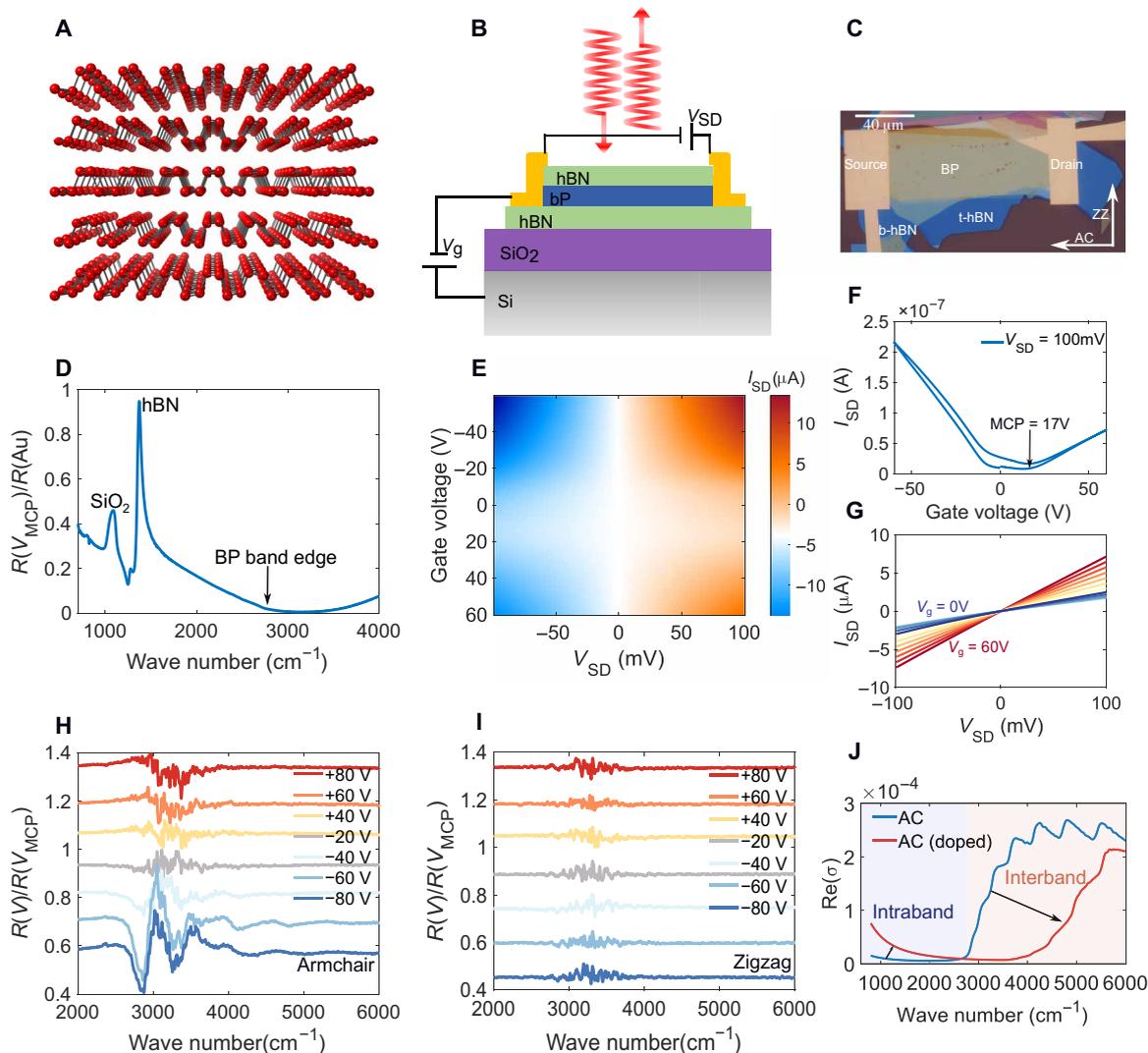


Fig. 1. Device schematic and electro-optic characterization. (A) Anisotropic puckered crystal structure of BP (P atoms are in sp^3 hybridization). (B) Device schematic and measurement scheme for hBN-encapsulated BP devices. (C) Optical microscope image of the device discussed in the main text. (D) Normalized reflection spectrum from the BP device shown in (C). (E) Color map of source-drain current variation as a function of both gate voltage and source-drain bias. (F) Gate voltage modulated source-drain current at one representative source-drain voltage (100 mV). (G) Variation of source-drain current with source-drain voltage showing linear conduction with systematic increase as gate voltage increases on the positive side; the slight dip is due to the fact that the minimal conductance point (MCP) is not at 0 V. (H and I) Interband optical modulation along the armchair (AC) and zigzag (ZZ) axis, respectively, showing the anisotropy in the electro-optic effects. (J) Schematic of changes in the AC axis optical conductivity (real part) upon doping.

electron densities by performing reflection spectroscopy. Modulation of reflection was observed both above and below the BP band edge. While changes near or above the optical gap can be understood from an interplay of different electro-optic effects in BP (such as Pauli blocking, quantum confined Stark effect, etc.) and modeled using the Kubo formalism, modulation below the bandgap is attributed primarily to changes in the intraband optical conductivity that has a Drude-like frequency response ($\sigma = \frac{iD}{\pi(\omega + i\Gamma)}$). We measured the Drude weight (D) evolution and thus the change in the optical conductivity as a function of electron/hole concentration in the 2DEG. As predicted by theory, we observed anisotropy of the polarization-resolved Drude response due to the difference in the effective mass of carriers along the two principal crystal axes. Changes

in the intraband absorption imply a transfer of the spectral weight from the interband transitions, thereby preserving the oscillator f -sum rule for solid-state systems, $\int_0^\infty \Delta\sigma(\omega) d\omega = 0$. Last, from the extracted complex-polarized dielectric function for BP below the band edge, we were able to identify an ENZ-like regime along the armchair (AC) direction and, hence, a transition from dielectric- to metallic-like response. No such transition was seen for the zigzag (ZZ) direction, confirming that doped multilayer BP is an ideal system to host plasmons with tunable in-plane hyperbolic dispersion in the mid-IR. Furthermore, our results indicate a possible gate-tunable optical topological transition for transverse magnetic (TM)-polarized light from hyperbolic to elliptical, which suggests interesting opportunities for multilayer BP in mid-IR photonic applications (50).

RESULTS

Optical and electrical characterization of multilayer BP field-effect heterostructure

We used Fourier-transform IR micro-spectroscopy to measure reflection spectra of multilayer BP structures. A typical field-effect heterostructure, schematically illustrated in side view in Fig. 1B, constructed using van der Waals assembly technique, is shown in Fig. 1C, where the BP is 18.7 nm and the top and bottom hBNs are 36.8 and 36.4 nm, respectively. The carrier density in BP was tuned by applying a gate voltage across the bottom hBN and SiO₂ (285 nm). Such a geometry allowed independent electrical and optical characterization of the induced 2DEG in BP. Polarized Raman spectroscopy was used to identify the AC and ZZ axes of BP as indicated in the optical image of the device. All optical and electrical measurements were performed in ambient at room temperature.

The reflection spectrum, shown in Fig. 1D, for the same device was measured at the minimal conductance point (MCP), confirmed from two-terminal electrical measurements as shown in Fig. 1 (E to G), with light polarized along the AC direction. This spectrum is normalized to that of optically thick Au (approximately 500 nm) evaporated on the same sample as a reference surface. Three prominent features dominate the spectrum—a narrow hBN phonon around 1370 cm⁻¹, a broad dominant SiO₂ phonon around 1100 cm⁻¹ [recent studies (15) show multiple phonon contributions in SiO₂], and the beginning of band edge absorption around 3000 cm⁻¹ convoluted with an interference dip coming from the entire stack. In addition, from our transport measurements, a hole mobility of 1107 cm²/V·s and an electron mobility of 412 cm²/V·s were obtained at low doping levels, corresponding to scattering rates on the order of approximately 5 to 10 meV. A separate figure in the Supplementary Materials shows the spectral features from interband absorption for multiple subbands. As shown in Fig. 1 (H and I), these reflection spectra can be heavily modified under positive or negative gate voltages.

Modeling the optical conductivity of the BP electron/hole gas allows us to gain an understanding of the quasiparticle dynamics under applied voltage. Our BP flakes are between 10 and 20 nm thick and described by a sheet conductivity σ since the effective modulation is confined to only 2 to 3 nm from the interface of BP/b-hBN. The thickness of this modulated region was estimated from the results of band bending calculations, which are detailed in the Supplementary Materials. This sheet conductivity has contributions from both interband and intraband processes, given as $\sigma = \sigma_{\text{interband}} + \sigma_{\text{intra}} = \sigma_1(\omega) + i\sigma_2(\omega)$. The interband contribution accounts for absorption above the band edge, including all subbands, while the intraband part accounts for free-carrier response. One can explicitly calculate for optical conductivity using the Kubo formalism as follows (48)

$$\sigma_{\text{interband}} = -i \frac{g_s \hbar e^2}{(2\pi)^2} \sum_{ss'j'j} \int dk \frac{f(E_{sjk}) - f(E_{s'j'k})}{E_{sjk} - E_{s'j'k}} \frac{\langle \phi_{sjk} | \hat{v}_\alpha | \phi_{s'j'k} \rangle \langle \phi_{s'j'k} | \hat{v}_\beta | \phi_{sjk} \rangle}{E_{sjk} - E_{s'j'k} + \hbar\omega + i\eta} \quad (1)$$

$$\sigma_{\text{intra},j} = \frac{iD_j}{\pi(\omega + \frac{i\eta}{\hbar})}, D_j = \pi e^2 \sum_{i=1}^N \frac{n_i}{m_{i,j}^*} \quad (2)$$

Here, $\hat{v}_{\alpha,\beta}$ is the velocity operator defined as $\hbar^{-1} \partial_{k_{\alpha,\beta}} H$, $g_s = 2$ is used to denote the spin degeneracy, and $f(E)$ is the Fermi-Dirac distribution function; the indices $s(s')$ refer to conduction (valence) bands and the indices $j(j')$ refer to the subbands. H is the low-energy in-

plane Hamiltonian around the Γ point, and E_{sjk} and ϕ_{sjk} are the eigenenergies and eigenfunctions of H ; $m_{i,j}^*$ represents the effective mass of carriers in each subband (i) along a specific crystal orientation j , n_i represents the charge density in each subband, and η is a phenomenological damping term.

Electrostatic doping of BP primarily brings about two fundamental changes in the optical response: the emergence of a strong intraband component in the mid- to far IR and a shift of the optical gap (interband transitions), shown schematically in Fig. 1J. A combination of multiple electro-optical effects at the band edge has been shown to explain the observed modulation (more details are available in the Supplementary Materials). All of the observed reflection modulation spectra exhibit strong anisotropy with respect to the BP crystal axes under AC- and ZZ-polarized illumination. This strong anisotropy is predicted by theory and results from the puckered honeycomb lattice crystal structure of phosphorene (51). Our results in Fig. 1 (H and I) indicate strong optical modulation in the 2DEG and are in excellent agreement with results from previous studies (40–43).

Low-energy doping-dependent intraband response in multilayer BP

We now turn our attention to the low-photon energy regime, which is dominated by the intraband conductivity of BP. Figure 2 describes this response, the understanding of which is a central result of this paper. Figure 2 (A and B) shows reflectance spectra (normalized as before) for light polarized along the AC and ZZ axes, respectively. Both electron and hole doping can modify the free-carrier response of the 2DEG. As doping increases, a strong spectral feature is observed to appear around the characteristic hBN (~1360 cm⁻¹) and SiO₂ (~1100 cm⁻¹) intrinsic phonon peaks with both electron and hole doping. We propose that this feature results from an increase in the free-carrier density, which increases the Drude conductivity and thus modifies the optical properties of BP. This broad intraband modulation interferes with the previously described hBN/SiO₂ phonons, giving rise to an absorption line shape with a Fano-like modulation in the hBN/SiO₂ phonon regime. We hypothesize that this asymmetric Fano-like resonance shape (52, 53) indicates optical coupling between the narrow phonon resonances and the weak free-carrier absorption continuum. To better understand the nature of the line shape, we performed thin-film transfer matrix calculations to fit the spectra and account for multiple reflections and interferences in the heterostructure stack. Our model incorporates a Drude-like function for the intraband optical conductivity of the BP 2DEG, given by Eq. 2, with which we are able to extract the Drude weight as a function of doping. Assuming a simple parallel plate capacitor model, we can estimate the doping density at each gate voltage. For undoped BP, we assume a charge density of 10¹¹/cm² to account for the finite MCP response (coming from any defects or trapped charges). The contribution to the linewidth of the imaginary component of Drude conductivity from dephasing associated with finite scattering times was assumed to be on the order of that obtained from DC transport measurements (approximately 5 meV), which is a valid approximation in the energy ranges considered here. The possible sources of scattering include electron-phonon coupling, electron-electron repulsion, and interaction with defects and impurities. Studies have shown that crystals of layered materials on substrates with strong phonons can also show losses from electron-surface polar phonon

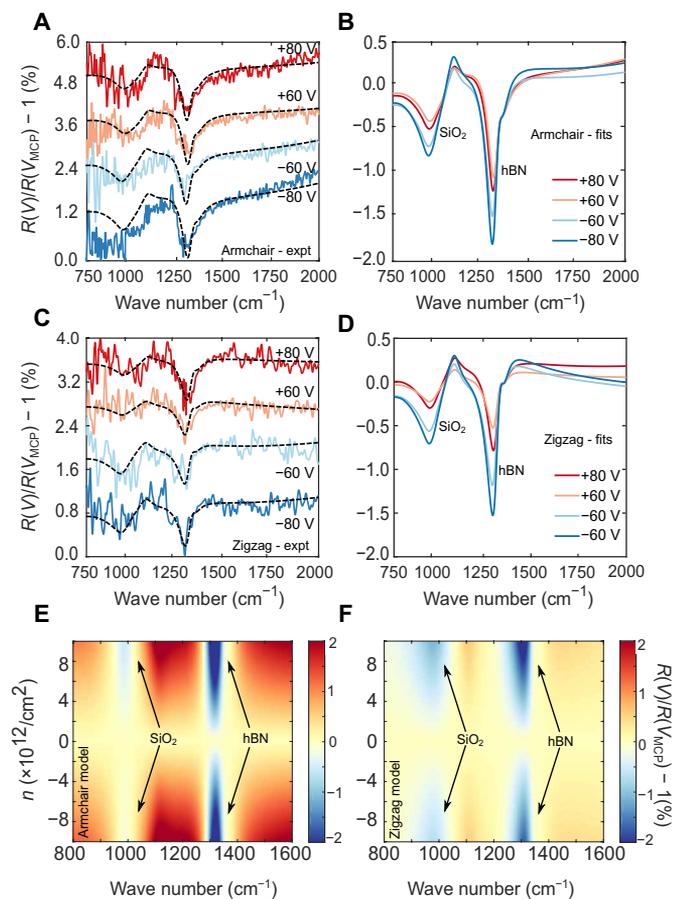


Fig. 2. Intraband response dominated reflection modulation. (A and C) Measured (colored lines) and simulated/fit (black lines) intraband response mediated reflection modulation along the AC and ZZ axes. The fits have been performed between 750 and 2000 cm⁻¹ to eliminate any band edge effect influence on the optical conductivity so that the Drude model suffices. (B and D) Fits shown separately, without offset showing a narrowing and strengthening of the Fano-like response near the hBN and SiO₂ phonons with increasing charge density in BP. (E and F) Modeled false-color plot of modulation in reflection spectra (zoomed in between 800 and 1600 cm⁻¹) as a function of doping density for the AC and ZZ directions assuming the following parameters: BP $m_{\text{eff}} = 0.14 m_0$ (AC), $0.71 m_0$ (ZZ), and Si $m_{\text{eff}} = 0.26 m_0$ (electrons) and $0.386 m_0$ (holes).

coupling (54). There have also been reports of DC transport mobilities that are not well correlated with optical scattering times, or which even show an anti-correlation (55). Further fundamental spectroscopic studies at far-IR (terahertz) frequencies will be required to further elucidate these low-energy scattering mechanisms in BP as a function of doping and temperature. Figure 2 (C and D) summarizes the fitted results without any offset to better understand the impact of doping on the lineshape of reflectance modulation. Excellent agreement between experimental data and transfer matrix simulations is visible in Fig. 2 (A and B), which indicates that the intraband (Drude) model suffices to explain the reflectance modulation observed at photon energies well below the band edge. Figure 2 (E and F) also shows in false colors the changes in the reflection modulation for AC and ZZ polarization as a function of electron/hole doping density assuming a constant effective mass for BP. Reflection/transmission in highly sub-wavelength BP films is mostly

dominated by the losses in the material, and thus, it is important to note that we do not incorporate the interband region in our Drude modeling of the sub-bandgap response because we are working much below the (even the Stark shifted) bandgap, where the influence of interband losses is almost negligible to first order. Similar assumptions have been experimentally validated for studies on graphene (49, 56). Also, it should be noted that while the interband anisotropy is primarily governed by the parity of wave functions and subsequent selection rules coming from dipole matrix elements in BP, intraband anisotropy stems from the difference in fermionic effective mass along the two crystallographic axes.

Measurement of the multilayer BP complex permittivity and tunable ENZ and hyperbolicity

Figure 3 (A to D) illustrates the experimental real and imaginary parts (denoted as ϵ_1 and ϵ_2) of the dielectric function [obtained as $\epsilon_{AC/ZZ}(\omega) = \epsilon_{\infty(AC/ZZ)} + \frac{i\sigma_{AC/ZZ}(\omega)}{t\epsilon_0\omega}$, where t = thickness of the 2DEG (2.9 nm) and $\epsilon_{\infty(AC/ZZ)}$ accounts for oscillators not captured in our Drude spectral window] for BP at different doping densities under polarized excitation conditions along the AC and ZZ directions. At higher energies, the dielectric function is dominated by subband transitions whose oscillator strength diminishes upon doping primarily due to Pauli blocking, along with the aforementioned electro-optic effects. The lower-energy response is mostly dominated by free carriers. We observe a strong modulation of the dielectric function below the bandgap with doping density, indicating that free-carrier response is a significant effect in the mid-IR range. An important finding of our study is the appearance of an ENZ in BP for higher gate voltages/charge densities along the AC direction, where the real part of the permittivity transitions from positive to negative. A false-color plot showing the variation of the modeled real part of the dielectric permittivity with doping density along the AC direction is shown in Fig. 3E. The ENZ region is seen to systematically shift to higher photon energies with increased doping. Here, the effective mass of BP is assumed to be $0.14 m_0$, independent of doping density, for the sake of simplicity. No such negative permittivity region was identified for the ZZ direction measurements, implying extreme bianisotropy and the possibility to generate surface plasmon modes and in-plane hyperbolic photonic dispersion in BP. We further calculate the isofrequency contours for in-plane plasmons (TM-polarized surface modes) (10) for two different doping densities (one on the electron side and one on the hole side) at 750 cm⁻¹ to show that the hyperbolic dispersion is electrically tunable. Electrically tunable hyperbolic dispersion, illustrated in Fig. 3F, has intriguing implications, suggesting opportunities for active hyperbolic plasmonics and photonics. We note that the doping density achieved here is modest ($\sim 7 \times 10^{12}$ cm⁻²), and higher doping densities with larger κ dielectrics may enable the hyperbolic dispersion regime to move to shorter wavelengths. In the frequency regime accessible in our measurements, we do not observe a negative real permittivity along the ZZ direction, and we expect it to occur at much lower frequencies (< 500 cm⁻¹), which indicates that any surface plasmon modes at frequencies above 500 cm⁻¹ will inherit a hyperbolic dispersion (as shown in Fig. 3F), whereas those below will inherit an elliptical dispersion, thereby undergoing a topological transition in photonic dispersion. It should be possible to electrically tune the transition point, as indicated by our results. In addition, a Dirac-like dispersion [also known as a Dirac plasmonic point (57)]

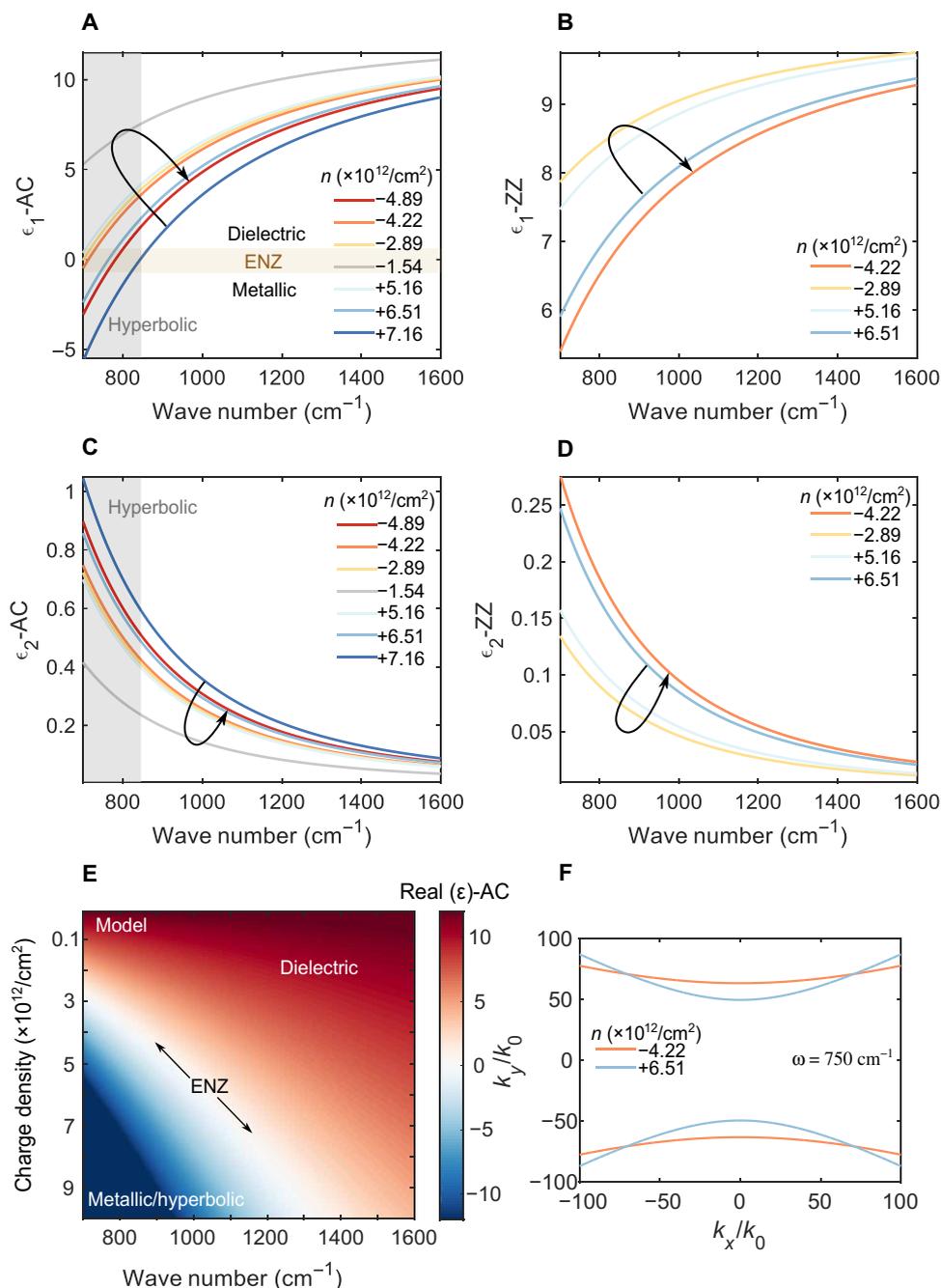


Fig. 3. Modeled dielectric function and tunable hyperbolicity. (A and C) Extracted real and imaginary part (denoted as ϵ_1 and ϵ_2) of the dielectric function for BP 2DEG along the AC axis for different doping densities. The orange shaded region shows the ENZ behavior. The region where the real part of the permittivity along the AC axis goes negative while remaining positive for the ZZ direction is the hyperbolic region and extends to frequencies beyond our measurement window. (B and D) The same for the ZZ axis. (E) False-color plot of the modeled real part of the dielectric permittivity along the AC direction assuming BP $m_{\text{eff}} = 0.14 m_0$ showing the tunability of ENZ. (F) Calculated isofrequency contours for in-plane plasmonic dispersion (TM-polarized surface modes) showing the tunability of hyperbolicity.

can be engineered in the system at slightly lower frequencies than the spectral window accessed in our measurements and has been discussed in section S14. Theoretical studies of surface plasmons in BP and their corresponding dispersion relations have been discussed elsewhere (8); however, our results provide a concrete step in that direction.

Determination of carrier effective masses in a multilayer BP 2DEG

Last, we use our experimental results to obtain carrier effective masses that can be compared with results from theory as shown in Fig. 4 (A and B). We see qualitatively good agreement with theory ($m_{\text{eff}} \approx 0.14 m_0$) for our results along the AC axis; our extracted

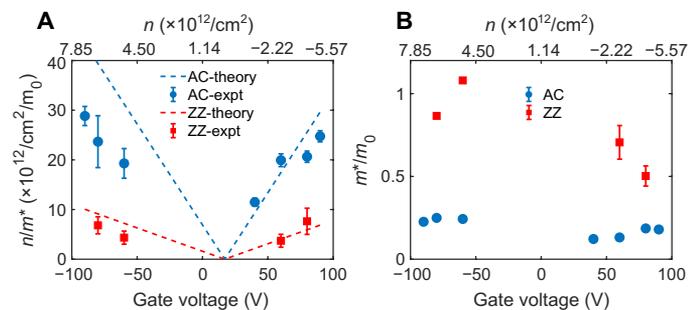


Fig. 4. Extracted Drude weight and effective mass for BP. (A) Drude weight evolution obtained from fitting reflection data for AC and ZZ axes, plotted with expected Drude weight. **(B)** Extracted effective mass from the Drude weight fits plotted versus voltage/charge density assuming a parallel plate capacitor model and 100% gating efficiency.

fermionic effective mass is slightly heavier than the previously theoretically calculated results. We speculate that this could be an interplay of two effects. First, in our BP thin films, the 2DEG is highly confined, and thus, the band dispersion is modified, leading to heavier confined fermions (28). In addition, when the Fermi level moves into either the conduction or valence band with gating, we access not only the minima and maxima of the first subbands in the conduction and valence band, respectively, but also the higher subbands (because of the broad Fermi-Dirac tail at 300 K). In BP, for higher lying subbands along the AC axis, the effective mass increases gradually, as given by $m_{AC}^i = \frac{\hbar^2}{2\gamma^i + \eta}$, where δ^i is the subband

transition energy, γ denotes the effective coupling between the conduction and valence bands, and η is related to the in-plane dispersion of the bands (47, 48). It is possible that the carriers participating in the intraband transitions come from a mixture of the different subbands, thus leading to an overall lower perceived effective mass. For the ZZ axis ($m_{eff} \approx 0.71 m_0$), we see a slightly larger variation in the extracted effective mass between the electron and hole side. Electronic confinement leads to heavier fermions along the ZZ direction, which is in accordance with our optical measurements for hole conductivity. It is possible that non-parabolic band effects give rise to a slightly lower effective mass for electrons, but further detailed analysis is needed to resolve the observed electron-hole asymmetry. It should be noted that for the ZZ direction, the effective mass is not expected to depend on the subband index. As expected from theory, the ZZ carriers are found to be much heavier than carriers associated with transport along the AC direction. To verify all of our results, we performed similar measurements with an unpolarized beam on the same sample (presented in the Supplementary Materials). We see highly consistent and reproducible interband conductivity modulation effects for light polarized along the AC or ZZ axis. Below the band edge, we see a systematic strengthening of the Fano-like response for both electron and hole doping in the wavelength range near the hBN and SiO₂ phonons. Fits to those datasets are in excellent agreement with our theoretical analysis. In addition, we find that the effective mass obtained is approximately the average of the in-plane effective masses along the AC and ZZ directions. This indicates that carriers along both the axes participate in the intraband response and is consistent with BP transport measurements. Subtle deviations are expected to occur in the estimation of the effective

mass because of the nonsymmetric nature of the unpolarized beam in our setup (it is slightly elliptically polarized) and possibly because of complex cross-scattering mechanisms between the two crystallographic directions. Overall, both polarized and unpolarized measurements are in good agreement with theory. We note that it is difficult to eliminate small conductivity changes due to local fluctuations in the charge density arising from charge puddles (bubbles/grain boundaries/defects) in heterostructures since our measurements probe a large area (approximately $2500 \mu\text{m}^2$) (58). In addition, studies have shown some systems to have an energy-dependent quasiparticle scattering rate owing to strong electron-electron and electron-phonon interactions (59, 60). Such interactions can cause additional broadening in both the interband and the intraband absorption features and have not been considered in our data analysis. We also note that in thick BP films ($>5 \text{ nm}$) like those measured here, excitonic effects are negligible and hence have not been taken into account. We performed measurements on three other BP heterostructures and saw very similar behavior.

DISCUSSION

We have experimentally explored the below-bandgap optical response in gated multilayer BP heterostructures and identified the dominant contribution to be a Drude-like optical conductivity due to free carriers in the 2DEG. We find that interband transitions play a negligible role in the low-photon energy response for BP, which greatly simplifies modeling of the optical conductivity of BP 2DEGs and subsequent photonic devices. We have measured the anisotropy in the intraband optical conductivity of BP by performing polarized reflection measurements and extracted the effective masses along the two crystallographic axes as a function of charge density. Our intraband optical conductivity results are consistent with any changes in the interband regime and DC transport measurements. Moreover, we demonstrated the existence of a plasmonic regime with electrically tunable hyperbolic dispersion and an ENZ regime. We also identified the wavelength regime for the onset of a topological transition for BP surface plasmons between hyperbolic and elliptical dispersion. Our results provide a foundation for a range of future research directions investigating BP as a strongly bianisotropic (or hyperbolic) mid-IR material for applications such as plasmonics, molecular fingerprinting, sensing, and tailoring thermal emission. They also pose important questions about the different scattering mechanisms in BP amidst a complex phase space of doping, thickness, substrate, and temperature, and the nature of the mid-IR to terahertz response in BP, which motivates future work. Last, our demonstration of BP as a naturally occurring material with tunable hyperbolic dispersion and bianisotropy suggests applications in novel photonics such as active polarization-sensitive IR metasurfaces.

MATERIALS AND METHODS

Device fabrication

BP (crystals from hqgraphene) was exfoliated using blue Nitto tape onto polydimethylsiloxane (PDMS) stamps and suitable flakes were identified. Flakes were chosen on the basis of the following parameters: contrast in the false-color microscope images in transmission (lower-contrast flakes were thinner), size ($>30 \mu\text{m}$ by $30 \mu\text{m}$ for spectroscopic measurements), and shape (rectangular/square shapes with easily identifiable axes were chosen for ease of fabrication and

polarization measurements). Thin hBN flakes [bulk crystals from the National Institute of Materials Science (NIMS)] were exfoliated onto SiO₂/Si (double side polished) and identified on the basis of their colors. The thickness of each flake was later checked with atomic force microscopy (AFM). Large flakes of hBN were selected so that the BP would be fully encapsulated (this is important to prevent any ambient degradation of BP). Once the bottom hBN was identified, an appropriate BP flake was transferred from PDMS on to hBN using the dry transfer technique at 60°C slowly, ensuring a clean interface; the cleanliness of this interface is the most important since it hosts the 2DEG in BP. Another large BN flake was then picked up with polycarbonate (PC)/PDMS at 90°C and then dropped on the BP/hBN stack at 180°C slowly, ensuring that two edges of BP were exposed. For the device discussed in this paper, the exposed edges were along the AC direction for maximal functionality and accurate estimation of mobilities along the same. The PC was then washed off with chloroform for 10 min and isopropyl alcohol (IPA) for 30 s and dried with N₂. Polymethyl methacrylate 950A4 was spun at 3000 rpm for 1 min (thickness, ~200 nm) and then baked at 180°C for 3 min for electron beam lithography. Electrical contacts to the BP were written with electron beam lithography at an acceleration voltage of 100 keV and a beam current of 1 nA (area dosage of 1350 μC/cm²), developed in methyl isobutyl ketone:IPA 1:3 for 1 min and then rinsed in IPA for 30 s (followed by blow drying with N₂). Metal (Ti/Au 5 nm/95 nm) was evaporated at 0.5 Å/s and 1 Å/s, respectively, at a base pressure of 7 × 10⁻⁸ torr, ensuring electrical contact. All the processing steps were done inside the glovebox to prevent degradation, except the e-beam lithography and the step between developing the resist and metal evaporation. The time between developing and loading in the loadlock for metal evaporation was less than 2 min.

Measurements

Once the device fabrication was complete, the chip was wire-bonded onto a custom-made printed circuit board and mounted on a polarization-resolved Raman spectroscopy setup. Polarized Raman measurements were used to confirm the axes of BP. Two Keithley 2400s were used (automated with LabView scripts) for the DC transport measurements, which involved two different methods of measurement: (i) At a constant source-drain voltage, the gate voltage was swept from 0 up to the maximum positive voltage, back to 0, then to the negative maximum voltage, and then to 0 at 0.1 V/s. (ii) At a constant gate voltage, the source-drain voltage was swept in a similar fashion. Both modes of measurements show highly similar MCP and on/off ratios and linear source-drain transport showing ohmic contacts (at room temperature). Then, the printed circuit board was mounted onto a (Nicolet iS50) Fourier transform IR spectrometer coupled with an IR microscope setup. A 15× Cassegrain objective with numerical aperture = 0.58 was used for all the measurements. A KBr beam splitter was used for the interferometry, and a KBr wire-grid linear polarizer for polarization resolved reflection measurements. Reflection spectra were acquired using a liquid nitrogen-cooled HgCdTe detector from 600 to 8000 cm⁻¹ with a resolution of 4 cm⁻¹. The linear polarizer was used in the optical path before the sample to polarize the incident light along the two principal axes of BP. Voltage was applied with a Keithley 2400. During the optical measurements, the source and drain were held at the same voltage and the back gate voltage was systematically varied from -90 to +90 V (higher voltages were avoided to prevent damage to the device, but based on our previous experience, most of these

devices may survive up to much higher voltages since breakdown usually occurs above 120 to 140 V). The BP thickness was examined after all the measurements were done since we do not have an AFM in the glovebox. Good correlation was found between the optical contrast and AFM height checks. Also, the hBN top and bottom flakes were inspected with IR spectroscopy before the assembly of the device to extract the phonon parameters.

It should also be noted that for such long-wavelength IR measurements, systematic drifts in the system can lead to artificial features, and to eliminate any such effect, we adopted the following techniques: (i) After taking data at a specific voltage, the gate bias was taken to the MCP level and a spectrum was taken immediately, which served as a baseline/reference for that specific voltage. (ii) The manner in which voltages were scanned was completely randomized to ensure that the modulation seen is not a time-dependent drift in the system. (iii) The whole process was repeated on the same device four to five times to confirm a systematic change was seen.

SUPPLEMENTARY MATERIALS

Supplementary material for this article is available at <http://advances.sciencemag.org/cgi/content/full/7/2/eabd4623/DC1>

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