Refractive Index Modulation in Monolayer Molybdenum Diselenide
Melissa Li, Souvik Biswas, Claudio U. Hail, and Harry A. Atwater*

ABSTRACT: Two-dimensional transition metal dichalcogenides are promising candidates for ultrathin light modulators due to their highly tunable excitonic resonances at visible and near-infrared wavelengths. At cryogenic temperatures, large excitonic reflectivity in monolayer molybdenum diselenide (MoSe₂) has been shown, but the permittivity and index modulation have not been studied. Here, we demonstrate large gate-tunability of complex refractive index in monolayer MoSe₂ by Fermi level modulation and study the doping dependence of the A and B excitonic resonances for temperatures between 4 and 150 K. By tuning the charge density, we observe both temperature- and carrier-dependent epsilon-near-zero response in the permittivity and transition from metallic to dielectric near the A exciton energy. We attribute the dynamic control of the refractive index to the interplay between radiative and non-radiative decay channels that are tuned upon gating. Our results suggest the potential of monolayer MoSe₂ as an active material for emerging photonics applications.

KEYWORDS: 2D materials, transition metal dichalcogenides, monolayer semiconductor, optical modulator, tunable optical properties, photonics

INTRODUCTION

Two-dimensional (2D) materials have attracted a great deal of attention over the past decade due to the new physics that emerges as the materials transition from bulk to monolayer. Particularly, transition metal dichalcogenides (TMDCs) such as MoSe₂ exhibit fundamentally distinct electronic and optical properties as the material evolves from indirect to direct band gap in the monolayer limit. As a result, the optical response of TMDC monolayers is dominated by strong excitonic resonances, which are highly tunable with external electric field or doping, dielectric environment engineering, and strain. Suppression of the excitonic response has previously been shown to modulate the refractive index of WS₂ at room temperature, but the non-radiative broadening at room temperature limits the achievable tunability. By encapsulating TMDCs with hexagonal boron nitride (hBN) to produce high-quality heterostructures and operating at cryogenic temperatures, the excitonic line widths can be narrowed by over an order of magnitude.

Here, we study the optical response of monolayer MoSe₂ at different carrier densities and cryogenic temperatures. Compared to other TMDCs, the optical properties of MoSe₂ at low temperatures have significantly less contributions from defects, allowing more accurate characterization of changes in the optical response. We exploit the narrow line widths of the excitons at low temperatures and show that Fermi level control via electrical gating of carrier density gives rise to large refractive index modulation at both the A exciton and B exciton energies. At temperatures between 4 and 150 K, we observe an epsilon-near-zero (ENZ)-like regime and hence a transition from metallic to dielectric near the A exciton energy, resulting in large changes in reflectance amplitude and phase. We note that while the temperature- and voltage-dependent

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reflectances have been previously shown\textsuperscript{24,25} the gate-tunability of the complex refractive index has not been studied in these TMDCs at cryogenic temperatures. In applications where electro-optic modulation is used to tune the scattering response of nanophotonic structures near excitonic and geometrical resonances, it is important to characterize the complex refractive index changes accompanying the observed reflectance modulation.\textsuperscript{26,27} Our demonstration of refractive index tunability indicates the possibility to manipulate light with monolayer 2D materials for ultra-thin optical modulators.

\section*{RESULTS}

We measure the gate-dependent reflectance spectra of a monolayer MoSe\textsubscript{2} device at cryogenic temperatures using a broadband white light source. The schematic and microscope images of the device are shown in Figure 1a,b. The device consists of an MoSe\textsubscript{2} monolayer encapsulated between top hBN (5.2 nm) and bottom hBN (25 nm), which passivates the MoSe\textsubscript{2} monolayer to enhance the carrier mobility and reduces the line width.\textsuperscript{21–23,28} A bottom few-layer graphene flake serves as the back electrode to control the carrier density in the MoSe\textsubscript{2}. The entire heterostructure, fabricated with an all-dry transfer technique, is placed on an SiO\textsubscript{2}/Si substrate with pre-patterned gold electrodes to contact the MoSe\textsubscript{2} and graphene. The carrier density in MoSe\textsubscript{2} is tuned by applying a gate voltage across the bottom hBN, which acts as the capacitor between the graphene and MoSe\textsubscript{2}. To obtain the absolute reflectance of the TMDC heterostructure, the spectrum is normalized to that of an optically thick gold layer adjacent to the sample.

The gate-dependent excitonic features of MoSe\textsubscript{2} are shown in both photoluminescence (PL) and reflectance spectra in Figure 1c,d. At 4 K, we observe two main features in PL that are associated with the A exciton and trion resonances at wavelengths of 757 and 769 nm, respectively. However, in reflectance, we observe three features associated with the A exciton, trion, and B exciton resonances. The presence of A and B excitons is attributable to the spin–orbit coupling induced valence and conduction band splitting.\textsuperscript{29} We note that our PL spectrum does not contain a prominent B exciton feature, presumably because the PL quantum yield is lower than that of the A exciton. Moreover, we observe two main differences in the trion features when comparing the PL and reflectance measurements. First, at 0 V, we observe a stronger PL signal from the trion compared to the A exciton, whereas in reflectance, the A exciton feature is dominant. This difference is commonly seen at 4 K in MoSe\textsubscript{2} and can be explained by the low oscillator strength of trions.\textsuperscript{30,31} While the oscillator strength of a transition is intimately related to the radiative lifetime and PL intensity, the one-to-one correspondence is not typically observed due to the band structure and additional relaxation channels. The trion exists at a lower energy than the A and B excitons, and the PL emission favors the lowest energy state. Therefore, even though the trion has low oscillator strength and, hence, low absorption, when the sample is excited above the A and B exciton energies with a 532 nm laser, we see a strong trion PL contribution from the relaxed A and B exciton states.

Furthermore, we observe a difference in the energy shift direction of the trion when the sample is electron doped, which corresponds to positive voltages in our electrostatic gating scheme. In reflectance, we see that the peak energy of the trion feature blueshifts, but in PL, the peak energy redshifts. To understand this finding, we consider the different mechanisms that can influence the reflectance and PL spectra.\textsuperscript{32–34} Reflection can be affected by Pauli blocking upon doping, leading to an increase in the effective optical gap which results in a blueshift. However, PL involves recombination of electron–hole pairs that relax to the band edges, resulting in the Stokes shift which increases with doping.
Another possible explanation for this difference in the energy shifts in PL and reflectance is that the quasiparticle associated with the lower energy peak is potentially an attractive polaron instead of a trion.30,35 However, here, we will refer to the lower energy feature as the trion for consistency.

We obtain the complex refractive index for MoSe2 by using a Kramers–Kronig consistent analysis and fitting the reflectance spectra of our entire heterostructure stack with the transfer matrix method to account for interference effects. We begin our analysis by modeling the dielectric function of the monolayer as a sum of Lorentz oscillators:36

\[
\tilde{\epsilon} = \epsilon_\infty + \sum_j \frac{f_j}{E_j^2 - \epsilon^2 - i\gamma_j} 
\]

Here \(\epsilon_\infty\) is the background MoSe2 dielectric constant and \(f_j, E_j, \gamma_j\) are the oscillator strength, resonant energy, and line width of the \(j\)th oscillator, respectively. In our analysis, each oscillator represents an individual excitonic or trionic feature. The complex refractive index is then calculated from the fitted dielectric function as follows: \(n = n + ik = \sqrt{\tilde{\epsilon}}\). We note that this method of obtaining the refractive index has been previously demonstrated to give accurate results for TMDC.

Figure 2. Gate-dependent reflectance spectra and refractive index at \(T = 4\) K. (a) Reflectance spectra of monolayer MoSe2 at 4 K for different gate voltages. The colored points are experimental data from line cuts of different voltages from Figure 1d. The solid black lines are fits from transfer matrix calculations where the MoSe2 dielectric function is modeled using the multi-Lorentzian model. The spectrum corresponding to \(-6\) V shows the absolute reflectance values, and the spectra at higher voltages are offset for clarity. (b) Fitted real \((n)\) and imaginary \((k)\) parts of the refractive index with different voltages. (c) Changes in the real and imaginary parts as a function of electron carrier density for four different wavelengths.

Figure 3. Gate-tunability of exciton parameters and ENZ response at \(T = 4\) K. (a) Change in oscillator strength, resonance wavelength, and oscillator line width for the A exciton, B exciton, and trion as a function of electron carrier density. (b) Schematic of electronic band structure, allowed transitions, and competing electronic effects for different Fermi levels. (c) Real part of the dielectric permittivity as a function of wavelength and carrier concentration. Near the A exciton resonance (754 nm), the MoSe2 undergoes a transition from optically metallic to optically dielectric.
monolayers from reflectance measurements at room temperature. The gate-dependent real and imaginary parts of the refractive index are shown in Figure 2b. By comparing the experimental results with the corresponding fitted gate-dependent reflectance, we see that modeling the MoSe$_2$ dielectric function with three oscillators yields an excellent fit to the data (Figure 2a). The refractive index near both the A exciton and B exciton energies shows extremely large gate tunability. At 748 and 754 nm, both the real and imaginary parts can be tuned by over 200% compared to their values at the charge-neutral point, where the gate voltage $V = -2.5$ V maximizes the exciton signal (Figure 2c). We note that this refractive index modulation is over 5 times larger than previously reported for both the real and imaginary parts in TMDCs. To better understand the mechanisms for the large refractive index modulation, we study the effects of carrier density on the oscillator strength, line width, and peak energy of the three excitons. The resulting fitting parameters for each oscillator as a function of carrier density are shown in Figure 3a. For negative voltages, the changes in the oscillator strength, line width, and peak energy are negligible since the hole doping is less efficient and presumably the semiconductor resides in a more “intrinsic” regime. However, for electron doping, we see an exchange of oscillator strengths between the A exciton and trion and a reduction in the oscillator strengths for both the A and B excitonic features. For the line width and peak energy behaviors, the A exciton and trion features are noticeably different from the B exciton feature. Figure 3a shows that the line widths of the A exciton and trion both broaden monotonically with carrier density, while the B exciton initially broadens up to a certain doping density and then narrows. Moreover, the peak energies for both the A exciton and trion blueshift, while that for the B exciton redshifts.

The striking differences in line width variation and energy shifts can be explained by considering the electronic band structure of MoSe$_2$ along with the effects of Coulomb scattering, screening, and Pauli blocking (Figure 3b). First, the screening of the electric field due to increased free carriers reduces the strength of the Coulomb interaction for the exciton. This leads to an overall decrease in the oscillator strength for both the A exciton and B exciton, attributable to a reduction in the binding energy. We note that while the trion oscillator strength increases due to a higher probability of formation in the presence of excess charges, the overall sum of A exciton and trion oscillator strengths decreases, which is consistent with the effects of screening and reduced Coulomb interactions. Second, for the A exciton and trion, the Coulomb scattering leads to a decrease in the coherence lifetime, resulting in spectral broadening of both transitions. The behavior at the B exciton energy is likely due to an emergence of charged B excitons at low electron densities, where the total line width initially broadens due to contributions from both the neutral and charged B excitons. At higher electron densities, the neutral exciton vanishes, leading to a decrease in the total line width. However, the energies of the neutral and charged B excitons are close and are not spectrally resolved in the measurements, so only the combined contribution is...
Figure 5. Change in phase as a function of wavelength and voltage for 4 K. (a) Calculated phase shift spectra from $V = -2.5$ V using extracted $n$, $k$ values around the A exciton energy. (b) Comparison between calculated phase shift from $n$, $k$ and measured phase shift from fringe shift measurements for 754 and 750 nm.

considered in Figure 3a. Finally, Pauli blocking typically leads to a decrease in the binding energy due to the occupation of electronic states and the fermionic nature of electrons. Therefore, when the Fermi level is between the conduction bands, the A exciton and trion features will blueshift. However, the B excitons are only influenced by screening effects, which lead to redshifts from the re-normalization of the bandgap to lower energies.

Next, we explore the tunability of the ENZ and negative $\epsilon_1$ behavior of MoSe$_2$ at low temperatures. We note that, in previous reports of gate-dependent index modulation in TMDCs, the real parts of the dielectric functions have been strictly positive, and the negative permittivity and ENZ properties in MoSe$_2$ have not been examined or observed in either monolayer or multilayer MoSe$_2$. In Figure 3c, we observe that, near the A exciton resonance, the real part of the dielectric function becomes negative when the sample is hole doped or nearly intrinsic. As the electron density increases, the dielectric function approaches the ENZ regime and becomes positive over the entire spectral range. Moreover, we observe a spectral shift of the ENZ regime that results from the blueshift of the A exciton resonance.

Whether $\epsilon_1$ takes positive or negative values can be attributed to three main factors. As mentioned previously, the first attribute is the background dielectric constant ($\epsilon_{\infty}$) that shifts $\epsilon_1$ to a higher positive value. This is primarily dependent on the bulk properties of MoSe$_2$ and does not depend on the A exciton properties. The second and third factors are the oscillator strength and the line width of the exciton resonance, where larger oscillator strengths and narrower line widths result in a significant increase in $\epsilon_1$ and allow $\epsilon_1$ to become negative. This can be shown through comparing the carrier-density-dependent exciton properties in Figure 3a with the corresponding $\epsilon_1$ in Figure 3c. When the electron density reaches around $4 \times 10^{12}$/cm$^2$, the A exciton oscillator strength noticeably decreases and the line width broadens, which also corresponds to the doping density where $\epsilon_1$ becomes positive.

We perform the same gate-dependent measurements and analyses at higher temperatures of 50, 100, and 150 K (Figures S1–S5). The temperature-dependent real and imaginary parts of the dielectric function and the corresponding reflectance spectra at the charge neutral point are shown in Figure 4a,b, respectively. While the increase in temperature allows for an additional line width broadening mechanism, even at these higher temperatures, $\epsilon_1$ can attain negative values if the A exciton line width is around 13.2 meV or lower (Figure 4c). At 150 K, the line width is around 13.1 meV at charge neutrality, corresponding to a small negative value of $\epsilon_1 = -0.4$. Furthermore, by comparing Figure 4c and Figure 4e, we see that, at each temperature, the carrier density that gives rise to line widths broader than 13.2 meV also corresponds to the carrier density where $\epsilon_1$ crosses the ENZ regime and switches from negative to positive.

From the gate-dependent index behavior, we calculate the corresponding change in the phase of the reflected light off an isolated monolayer MoSe$_2$. The resulting phase modulations as functions of wavelength, voltage, and temperature are shown in Figures 4d and S6. We observe the largest overall change in the phase at 4 K, where $\Delta \Phi = 115^\circ$. We attribute this large tunability as a result of the narrower line widths at lower temperatures, which gives rise to a larger refractive index change around the resonance energies.

As a proof-of-concept demonstration of phase modulation, we directly measure the phase shift of the reflected light under applied bias by using an interferometer measurement where the laser light illuminates the edge of our monolayer flake. Therefore, a portion of the incident beam is reflected from the monolayer flake, while another portion is reflected from the substrate, which acts as a built-in phase reference. We then fit intensity profiles obtained from the images of the recorded interference fringes to sinusoidal functions, as shown in Figure S11, and calculate the relative displacement of the interference fringes originating from the sample and the back reflector reference with applied bias. Our measured phase shifts obtained directly from fringe shift measurements are in good agreement with the phase shift extracted from the refractive index values at wavelengths corresponding to both the excitonic resonance and off resonance (Figure 5a,b). At 754 nm, where the change in refractive index is maximal, we observe over a $25^\circ$ phase shift. We note this phase shift is observed in the absence of coupling to antennas or cavities, which is an important quantity for applications such as active metasurfaces. By integration of gated monolayer MoSe$_2$ with a cavity or metasurface, we find that the phase shift can be increased to over $270^\circ$, as illustrated in Figure S12.

So far, we have considered how the oscillator strength and line width change as a function of carrier density and temperature. However, these parameters can be directly related to the radiative $\gamma_r$ and non-radiative decay rates $\gamma_{nr}$ of the excitons by rewriting the dielectric function to take the form

$$\epsilon_1 = \frac{n^2 - k^2}{n^2 + k^2} + \frac{4\pi n k}{c} \frac{\omega^2}{\omega^2 - \omega_{\text{exc}}^2}.$$
In summary, we show remarkable tunability in the complex refractive index of MoSe$_2$ at both the A and B exciton energies, highlighting its potential for use as a reconfigurable active element in optoelectronic systems, including modulators and active metasurfaces. We find that both temperature and Fermi level modulation leads to an ENZ behavior, resulting in a transition from dielectric to metallic, accompanied by large changes in reflectance amplitude and phase. The large permittivity and index modulation result from Pauli-blocking, Coulomb scattering, and screening, which directly influence the radiative and non-radiative channels, oscillator strengths, and resonance line widths. Our findings of large electrical tunability provide a route for exploring novel phenomena and device applications based on monolayer TMDC excitons.

**CONCLUSIONS**

In summary, we show remarkable tunability in the complex refractive index of MoSe$_2$ at both the A and B exciton energies, highlighting its potential for use as a reconfigurable active element in optoelectronic systems, including modulators and active metasurfaces. We find that both temperature and Fermi level modulation leads to an ENZ behavior, resulting in a transition from dielectric to metallic, accompanied by large changes in reflectance amplitude and phase. The large permittivity and index modulation result from Pauli-blocking, Coulomb scattering, and screening, which directly influence the radiative and non-radiative channels, oscillator strengths, and resonance line widths. Our findings of large electrical tunability provide a route for exploring novel phenomena and device applications based on monolayer TMDC excitons.

**ASSOCIATED CONTENT**

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.nanolett.1c02199.

Additional experimental and simulation details, materials, and methods, including Figures S1–S13 with fringe images and interferometry data (PDF)

**AUTHOR INFORMATION**

Corresponding Author

Harry A. Atwater — Thomas J. Watson Laboratory of Applied Physics, California Institute of Technology, Pasadena, California 91125, United States; orcid.org/0000-0001-9435-0201; Email: haa@caltech.edu

Authors

Melissa Li — Thomas J. Watson Laboratory of Applied Physics, California Institute of Technology, Pasadena, California 91125, United States; orcid.org/0000-0003-1534-4191

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